

# **Residual Stresses in Welding: Some Experimental and Numerical Studies**

*A Thesis*

*Submitted in partial fulfilment*

*For the award of degree of*

*Doctor of Philosophy*

By

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**June, 2014**

**To**  
**My father**

## **APPROVAL OF THE VIVA-VOCE BOARD**

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## **DECLARATION**

I certify that

- a) The work contained in the thesis is original and has been done by myself under the general supervision of my supervisor.
- b) The work has not been submitted to any other Institute for any degree or diploma.
- c) I have followed the guidelines provided by the Institute in writing the thesis.
- d) I have confirmed to the norms and guidelines given in Ethical Code of Conduct of the Institute.
- e) Whenever I have used materials (data, theoretical analysis and text) from other sources I have given due credit to the by citing them in the text of the thesis and giving their details in the references.

**Date:**

**(Dhanyamraju V N J Jagannadha Rao)**

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## ABSTRACT

The intense localized heating and cooling in the fabrication of welded joints leads to residual stresses and distortion which reduce the service life of the joint. The prediction and mitigation of residual stresses is as important task in the design and fabrication of the joint. Prediction of residual stresses requires solution to a non-linear transient thermo-elasto-plastic problem. The complicated physics of welding include material dependence on temperature, phase change, plasticity, filler metal addition and restraint.

In this work thermo-mechanical analyses of various welded components namely a square corner joint, butt welded plates, a tee panel, bead on pipe and spiral welded pipe are presented. The materials used are mild steel and C-Mn steel. Weld bead is modelled as circular arc with the initial temperature of the filler metal is at its melting temperature. Double ellipsoidal heat flux density distribution is used to model the heat input and filler element additions are made by element birth-death method in a transient thermal solution based on enthalpy. Rate independent kinematic hardening is used to model the plastic behaviour and the thermal load is calculated with the reference temperature of the base metal is at ambient temperature and that of filler metal is at melting temperature. The mechanical strains elastic strains and plastic strains are omitted from the analyses when the temperature of the metal is at or above the melting temperature.

Numerical solutions are obtained for temperature and residual stresses. Thermal histories at various locations of the welded components are measured with online thermocouple measurements and residual stresses at various locations of square corner joint and pipe are measured by X-ray diffraction. The comparison of computed thermal histories with experimental thermal histories yielded very good agreements. Experimental values of residual stresses are compared with the corresponding results of computed results. In bead on pipe welding both the hardening methods kinematic and isotropic hardening models resulted in almost identical values of residual stress distributions. Thermal histories and residual stresses of a typical spiral welded pipe are also presented. Further the effect of weld pass sequencing on residual stresses is investigated with weld



pass sequencing methods skip step, back step and normal weld pass sequencing methods. There is a good amount of reduction in the values of residual stresses and distortion with nonconventional weld pass sequencing methods with skip step weld pass sequencing offering least amount of residual stresses and distortion.

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## LIST OF SYMBOLS

### *Double ellipsoidal heat source*

$a, b, c_1, c_2$  are the parameters of the heat source in mm and  $f_r + f_f = 1$

$a_f$  = Front Ellipsoidal semi-axes length (mm)

$a_r$  = Rear Ellipsoidal semi-axes length (mm)

$b$  = Half width of arc (mm)

$c$  = Depth of arc (mm)

$f_f$  = Distribution factor in the forward direction of welding

$f_r$  = Distribution factor in the rear direction of welding

$I$  = Current (A)

$Q$  = Heat input ( $W/m^2$ )

$q$  = Heat flux density in  $W/m^3$

$q_f$  = Power density in front Ellipsoid ( $W/mm^3$ )

$q_r$  = Power density in rear Ellipsoid ( $W/mm^3$ )

$R_o$  = Pipe outer radius (mm)

$r$  = Radius of pipe (mm)

$r$  = Distance from centre of the arc in mm

$\bar{r}$  = Radius of arc in mm.

$t$  = Time in sec

$V$  = Voltage (V)

$v$  = Welding speed in mm/sec



$z$  = Distances from the torch centre in axial direction (mm)

$\eta$  = Efficiency of welding

$\theta$  = Angle from instantaneous arc position (radian)

### **Heat transfer coefficients**

$C_p$  = specific heat J/kgK

$D$  = diameter of the cylinder (m)

$Gr_L$  = Grashoff number

$h$  = Heat transfer coefficient (W/m<sup>2</sup>K)

$g$  = Acceleration due to gravity (m/s<sup>2</sup>)

$k$  = coefficient of thermal conductivity W/mK

$L$  = length of the plate (m)

$x, y, z$  = Cartesian co-ordinates

$\overline{Nu}_L$  = Average Nusselt number

$n_\lambda$  = thermal conductivity parameter

$n_\mu$  = viscosity parameter

$Pr$  = Prandtl number

$r, \theta, z$  = Cylindrical co-ordinates

$T_f$  = Temperature of the film (K)

$T_s$  = Temperature of the plate (<sup>0</sup>C)

$T_{\infty}$  = Ambient temperature ( $^{\circ}\text{C}$ )

$\beta$  = Volumetric coefficient of thermal expansion ( $1/\text{K}$ )

$\eta$  = dimensionless similarity coordinate variable

$\theta$  = dimensionless temperature variable

$\nu$  = Kinematic viscosity ( $\text{m}^2/\text{s}$ )

$\rho$  = density  $\text{kg}/\text{m}^3$

### ***FEM formulation***

$[B]$  = strain displacement matrix

$[C]$  = heat capacity matrix

$[D]$  = elasticity matrix

$[D]_s^{ep}$  = elasto – plastic tangent matrix

$\{\Delta d\}$  = incremental displacement

$F_{12}$  = shape factor

$\{F\}_n$  = external load

$\{f\}$  = load vector

$\{f\}_n$  = internal load

$\{f_p\}$  = point load vector

$\{f_{th}\}$  = thermal load vector

$\{f_w\}$  = body force vector

$\{f_{\epsilon 0}\}$  = initial strain vector load

$\{f_{\sigma 0}\} = \text{initial stress vector load}$

$H = \text{enthalpy}$

$h = \text{heat transfer coefficient } W/m^2K$

$[K] = \text{stiffness matrix, conductivity matrix}$

$[K]_n^{tan} = \text{tangent stiffness matrix at } n \text{ iteration}$

$[N] = \text{shape function matrix}$

$\{R\}_n^i = \text{residual at } i^{\text{th}} \text{ iteration}$

$\| R \| = \text{convergence norm}$

$S = \text{surface area } m^2$

$T = \text{temperature } ^\circ C$

$\{T\} = \text{temperature vector}$

$\{T\} = \text{traction force vector}$

$V = \text{volume } m^3$

$\Gamma = \text{boundary}$

$\{\delta\} = \text{displacement vector}$

$\epsilon = \text{emmissivity}$

$\epsilon = \text{convergence criterion, strain}$

$\{\epsilon\} = \text{total strain vector}$

$\{\epsilon^e\} = \text{elastic strain vector}$

$\{\epsilon^p\} = \text{plastic strain vector}$

$\{\epsilon^{th}\} = \text{thermal strain vector}$

$\{\epsilon^{ph}\} = \text{phase transformation strain vector}$

$\sigma = \text{stephen boltzman's constant}$

$\{\sigma\} = \text{stress vector}$

$\{\sigma_e\} = \text{elastic stress vector}$

$\{\sigma_0\} = \text{initial stress vector}$

$\Omega = \text{domain}$

### ***Radial Return Method***

$E = \text{elastic modulus}$

$F_n = \text{yield surface}$

$G = \text{shear modulus}$

$I = \text{second order identity tensor}$

$k = \text{bulk modulus}$

$tr = \text{trace}$

$\epsilon^d = \text{deviatoric strain}$

$\epsilon^e = \text{elastic strain}$

$\epsilon^h = \text{hydrostatic strain}$

$\epsilon^p = \text{plastic strain}$

$\epsilon_x, \epsilon_y, \epsilon_z = \text{normal components of strains}$

$\bar{\epsilon} = \text{effective strain}$

$\mu = \text{elastic constant}$

$\nu = \text{poisson's ratio}$

$\sigma = \text{stress}$

$\sigma^d = \text{deviatoric stress}$

$\sigma^h = \text{hydrostatic stress}$

$\sigma_x, \sigma_y, \sigma_z = \text{normal components of stresses}$

$\sigma_y = \text{yield stress}$

$\bar{\sigma} = \text{effective stress}$

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## LIST OF PUBLICATIONS FROM PRESENT RESEARCH

1. Jagannadha Rao D V N J and Biswas K. (2007). Temperature distribution in a welded corner joint: FEM prediction and its experimental verification. *Proceedings of International Conference on Advances in Manufacturing Technology*, Durgapur.
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