

---

## Table of Contents

<b>Abstract</b>	<b>i</b>
<b>List of Abbreviations</b>	<b>iii</b>
<b>Nomenclature</b>	<b>v</b>
<b>Chapter 1: Introduction</b>	<b>1</b>
1.1. Background and Motivation	1
1.2. Contributions of the Thesis	6
1.3. Organisation of the Thesis	7
<b>Chapter 2: Literature Survey</b>	<b>9</b>
2.1. Introduction	9
2.2. Bond Graph Modelling	9
2.3. Multibody Dynamics	11
2.4. Modelling of Stewart Platform	14
2.5. Bond Graph Modelling of Vehicles	16
2.5.1. Antilock Braking System	18
2.5.2. Regenerative Braking System	19
2.6. Simulation and Control of Stewart Platform	22
2.7. Objectives of the Present Work	25
<b>Chapter 3: Bond Graph Modelling of Multibody Dynamics</b>	<b>27</b>
3.1. Introduction	27
3.2. Planar Multibody Systems	29
3.2.1. Plane Impedance Model	29
3.2.2. Model of Rigid Planar Links	30
3.2.3. Model of Revolute Joints	32

3.2.4.	Model of the Slider Component	34
3.2.5.	Case Study: Rapson Slide	37
3.3.	Spatial Multibody Systems	42
3.3.1.	Cardan Angles	42
3.3.2.	Newton's Equations in Non-inertial Frame	43
3.3.3.	Euler's Equations	45
3.3.4.	Transformation of Linear and Angular Velocities	46
3.3.5.	Determination of Euler Angle Rates	48
3.3.6.	Implementation of Constraints	49
3.3.7.	Example Application: Model of a Spinning Top	49
3.4.	Conclusions	52
<b>Chapter 4: Modelling and Control of Stewart Platform</b>		<b>53</b>
4.1.	Introduction	53
4.2.	Modelling of Planar Stewart Platform	54
4.2.1.	Kinematic Analysis	55
4.2.2.	Bond Graph Model of Platform	57
4.3.	Modelling of Hydraulic Servo-System	59
4.3.1.	Four-way Directional Control Valve Model	59
4.3.2.	Modelling of Valve Flow Equation	60
4.3.3.	Bond Graph Model of Directional Control Valve	60
4.3.4.	Hydraulic Cylinder Model	62
4.3.5.	Formulation of the Constitutive Model	62
4.3.6.	Bond Graph Model of Hydraulic Cylinder	63
4.3.7.	PI Controller	66
4.4.	Overwhelming Controller as a System Inversion Tool	67
4.5.	Overwhelming Controller for Planar Stewart Platform	72
4.6.	Case Study–I: Virtual Reality Application	77
4.6.1.	A Planar Vehicle Simulator	78
4.6.2.	Simulation Results	80
4.6.3.	Noise-Sensitivity Study	82
4.7.	Case Study–II: Operation on a Plane Surface	85
4.7.1.	Trajectory Tracking Performance	86

4.7.2.	Effect of Leg Inertia	87
4.8.	Modelling of 3-D Stewart Platform	89
4.8.1.	3-D Stewart Platform Model without Leg Inertia	90
4.8.2.	3-D Actuator Model	91
4.8.3.	3-D Stewart Platform Model with Leg Inertia	94
4.9.	Inverse Model of 3-D Stewart Platform	97
4.10.	Conclusions	98
<b>Chapter 5: Application to Vehicle Simulator</b>		<b>99</b>
5.1.	Introduction	99
5.2.	Single Wheel Model	100
5.3.	Planar Bicycle Model	101
5.3.1.	Kinematic Relations	102
5.3.2.	Bond Graph Model	102
5.4.	Four Wheel Vehicle Model	103
5.4.1.	Word Bond Graph Representation	104
5.4.2.	Vehicle Body	105
5.4.3.	Suspension System and Axle	107
5.4.4.	Wheel	108
5.4.5.	Steering System	110
5.4.6.	Tyre Slip Forces and Moments	112
5.4.7.	Braking System	114
5.4.8.	Engine	129
5.4.9.	Differential	136
5.4.10.	Gearbox	136
5.4.11.	Integrated Vehicle Model with Transmission System	137
5.5.	Vehicle Dynamics Simulation	140
5.5.1.	Validation of Four Wheel Model	141
5.5.2.	Antilock Braking System in Four Wheel Model	142
5.5.3.	Sliding Mode Control in Four Wheel Model	143
5.6.	Stewart Platform for Vehicle Simulator	145
5.7.	Human-Machine Interface	147
5.8.	Graphics Interface	148

5.9. Results of Test Drive of Driving Simulator	150
5.10. Conclusions	155
<b>Chapter 6: Impedance Control of Stewart Platform</b>	<b>157</b>
6.1. Introduction	157
6.2. Design of Impedance Controller	158
6.2.1. Concept of Flexible Foundation	158
6.2.2. Concept of Virtual Foundation	161
6.2.3. Alternative Impedance Control Technique	161
6.2.4. Amnesia Removal	163
6.3. Force Controlled Machining with Stewart Platform	164
6.3.1. System Parameters and Initial Conditions	165
6.3.2. Trajectory Tracking Performance	165
6.3.3. Interaction Force Control	166
6.4. Conclusions	170
<b>Chapter 7: Conclusions</b>	<b>171</b>
<b>References</b>	<b>175</b>
<b>Appendices</b>	<b>187</b>
Appendix A Bond Graph Notations Revisited	187
A.1. Introduction	187
A.2. Causality	190
A.3. Activation	191
A.4. Sensors, Actuators and Instrumentation Circuits	191
A.5. Systems with Differential Causality	193
A.6. Field Elements	193
Appendix D List of Files and Programs Given in the Compact Disc	195
<b>Curriculum Vitae</b>	<b>197</b>