

# Contents

---

<b>Approval</b>	i
<b>Certificate</b>	iii
<b>Acknowledgement</b>	v
<b>Declaration</b>	vii
<b>Author's Resume</b>	ix
<b>Abstract</b>	xi
<b>List of Symbols</b>	xiii
<b>List of Figures</b>	xv
<b>List of Tables</b>	xix
<b>Chapter 1 Introduction</b>	1
1.1 General . . . . .	1
1.2 Review of Literature . . . . .	2
1.2.1 Multilayered Composite Shells . . . . .	3
1.2.2 Coupled Piezo-Elastic Smart Composite Shells . . . . .	11
1.3 Appraisal of the Past Work . . . . .	14
1.4 Objectives and Scope of the Present Work . . . . .	15
1.5 Organisation of the Thesis . . . . .	18

<b>Chapter 2 Theoretical Formulation</b>	<b>21</b>
2.1 Introduction . . . . .	21
2.2 Geometric Description of Shell . . . . .	22
2.3 Geometric Quantities Associated to Middle Surface . . . . .	22
2.4 Development of Shell Kinematics . . . . .	25
2.5 Strain Displacement Equations . . . . .	31
2.6 Electric Field- Electric Potential Relationship . . . . .	34
2.7 Constitutive Relations for Lamina . . . . .	35
2.8 Construction of the Mixed Functional . . . . .	38
2.9 Finite Element Equations . . . . .	44
2.10 Recovery of the Transverse Shear Stresses . . . . .	46
2.10.1 Recovery using Weighted Residual Method . . . . .	47
<b>Chapter 3 Bending of Composite Shells</b>	<b>49</b>
3.1 Introduction . . . . .	49
3.1.1 Abbreviations Used . . . . .	50
3.1.2 Shell Geometry Considered . . . . .	50
3.1.3 Geometric and Electrical Boundary Conditions . . . . .	52
3.1.4 Material Properties . . . . .	53
3.1.5 Non-dimensional Parameters . . . . .	53
3.2 Numerical Results . . . . .	53
3.2.1 Test for Rank Sufficiency . . . . .	54
3.2.2 Element Distortion Sensitivity and Convergence . . . . .	55
3.2.3 Sandwich Plates with Cross-ply Face Sheets . . . . .	59
3.2.4 Ren's Cylinder . . . . .	59
3.2.5 Cylindrical and Spherical Shell Panels . . . . .	61
3.2.6 Hyperbolic Paraboloidal Panels . . . . .	93
<b>Chapter 4 Bending of Smart Composite Shells</b>	<b>113</b>
4.1 Introduction . . . . .	113
4.1.1 Material Properties . . . . .	114
4.1.2 Non-dimensional Parameters . . . . .	114
4.2 Validation Problem-1: Analysis of a Sensor Plate . . . . .	114
4.3 Validation Problem-2: Analysis of a Actuator Plate . . . . .	115
4.4 Bending of a Four Layer Sensor Shell . . . . .	116
4.5 Static Analysis of a Four Layer Actuator Shell . . . . .	133

4.6 Seven Layer Smart Sandwich Shell under complex Loading . . . . .	155
<b>Chapter 5 Free Vibration of Smart Shells</b>	<b>165</b>
5.1 Introduction . . . . .	165
5.2 Validation of the Present Formulation . . . . .	165
5.3 Vibration of Laminated Composite Shells . . . . .	166
5.4 Vibration of Laminated Sandwich Shells . . . . .	171
5.5 Vibration of Four Layer Smart Shells . . . . .	171
5.6 Vibration of Seven Layer Smart Shells . . . . .	181
<b>Chapter 6 Critical Discussion and Concluding Remarks</b>	<b>183</b>
6.1 Introduction . . . . .	183
6.2 Critical Discussion of Results . . . . .	183
6.2.1 Bending of Composite and Sandwich Shells . . . . .	184
6.2.2 Bending of Smart Shells . . . . .	186
6.2.3 Vibrations of Smart Shells . . . . .	188
6.3 Concluding Remarks . . . . .	190
6.4 Contributions of the Present Thesis . . . . .	191
6.5 The Scope for Future Research . . . . .	192
<b>References</b>	<b>195</b>
<b>Appendix A</b>	<b>207</b>
A.1 Inertia Coefficients . . . . .	207
A.2 Element Mass Matrix . . . . .	207
A.3 Modified Subspace Iteration . . . . .	208